Simplify
(a)
$$(2\sqrt{5})^2$$

(a)
$$(2\sqrt{5})^2$$

(b) $\frac{\sqrt{2}}{2\sqrt{5}-3\sqrt{2}}$ giving your answer in the form $a+\sqrt{b}$, where a and b are integers.

a)
$$(2\sqrt{5})^2 = 2x\sqrt{5} \times 2 \times \sqrt{5} = 4 \times 5 = 20$$

b)
$$\sqrt{2}$$
 $\times (2\sqrt{5} + 3\sqrt{2})$ = $2\sqrt{10} + 3\times 2$
 $2\sqrt{5} - 3\sqrt{2}$ $\times (2\sqrt{5} + 3\sqrt{2})$ = $20 - 18$

$$2\sqrt{5} - 3\sqrt{2} \times (2\sqrt{5} + 3\sqrt{2}) \qquad 20 - 18$$

$$(3\sqrt{2})^{2} = 9 \times 2 = 18 \qquad = 2\sqrt{10} + 6 \qquad = \sqrt{10} + 3$$

Solve the simultaneous equations

$$y - 2x - 4 = 0$$

$$4x^{2} + y^{2} + 20x = 0$$

$$y = 2x + 4$$

$$y^{2} = (2x + 4)(2x + 4) = 4x^{2} + 16x + 16$$

$$2 + (4x^2 + 16x + 16) + 20x = 0$$

$$8x^{2}+36x+16=0 \quad (\pm 4) \quad 2x^{2}+9x+4=0$$

$$(2x+1)(x+4)=0 \quad x=-\frac{1}{2} \quad y=3$$

(7)

$$4x^{2} + (4x^{2} + 16x + 16) + 20x = 0$$

$$8x^{2} + 36x + 16 = 0 \quad (-4) \quad 2x^{2} + 9x + 4 = 0$$

$$(2x + 1)(x + 4) = 0 \quad x = -\frac{1}{2} \quad y = 3$$

$$x = -4 \quad y = -\frac{1}{2} \quad y = 3$$

 $(-\frac{1}{2},3)$; (-4,5)

3. Given that
$$y = 4x^3 - \frac{5}{x^2}$$
, $x \ne 0$, find in their simplest form

(a)
$$\frac{dy}{dx}$$

(a)
$$\frac{dy}{dx}$$

(b)
$$\int y dx$$

$$y = 4x^3 - 5x^{-2}$$

$$y = 4x^3 - 5x$$

$$4 = 12x^2 + 10x^2$$

$$= |2x^2 + 10x|$$

a)
$$\frac{dy}{dx} = 12x^2 + 10x^{-3} = 12x^2 + \frac{10}{x^3}$$

b) Jydx = 424 - Sx + c = 24+ 5 + c

(3)

(3)

(i) A sequence $U_1, U_2, U_3, ...$ is defined by

$$U_1 = 4$$
 and $U_2 = 4$

 $U_{n+2} = 2U_{n+1} - U_n, \quad n \geqslant 1$

(1)

(2)

(2)

(3)

Find the value of

Find the value of (a)
$$U_3$$

(b) $\sum_{n=0}^{20} U_n$

i) Another sequence
$$V_1, V_2, V_3, ...$$
 is defined by

(ii) Another sequence V_1 , V_2 , V_3 , ... is defined by

$$V_{n+2} = 2V_{n+1} - V_n, \quad n \geqslant 1$$

 $V_1 = k$ and $V_2 = 2k$, where k is a constant

$$V_1 = k$$
 and $V_2 = 2k$, w
(a) Find V_3 and V_4 in terms of k .

Given that
$$\sum_{n=1}^{5} V_n = 165,$$

(b) find the value of k.

a)
$$U_3 = 2U_2 - U_1 = 2(4) - 4 = 4$$

b)
$$\frac{20}{2}$$
 Un = $4 \times 20 = 80$

$$V_3 = 2V_2 - V_1 = 2(2u) - u = 3u$$

 $V_4 = 2V_3 - V_2 = 2(3u) - 2u = 4u$

b) 2 vn = 4+24+34+44+54 = 154 = 165 u=11

The equation

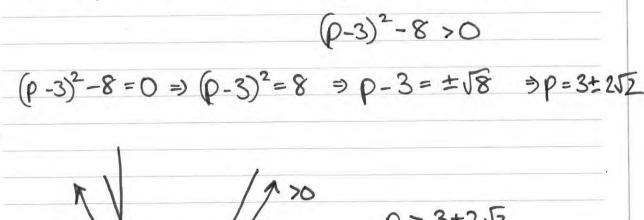
no real roots =>
$$b^2-4ac < 0$$

 $4^2-4(p-1)(p-s) < 0$
 $16-4p^2+24p-20 < 0 => 4p^2-24p+4>0$
 $\div 4$ $p^2-6p+1>0 => (p-3)^2-9+1>0$

blan

(3)

(4)



(a) Find $\frac{dy}{dx}$ in its simplest form.

Mt = -1 - 3 + 6 = = =

- The curve C has equation

 $y = \frac{(x^2 + 4)(x - 3)}{2x}, x \neq 0$

Give your answer in the form ax + by + c = 0, where a, b and c are integers.

=(1+4)(-1-3)=5x-4=10

(b) Find an equation of the tangent to C at the point where x = -1

(5)

(5)

(b) Hence, or otherwise, solve
$$8(4^x) - 9(2^x) + 1 = 0$$

(1)

(4)

Given that $y = 2^x$,

(a) express 4^x in terms of y.

a)
$$4^{x} = (2^{2})^{x} = 2^{2x} = (2^{x})^{2} = y^{2}$$

b)
$$8y^2 - 9y + 1 = 0$$

 $(8y - 1)(y - 1) = 0$

$$(8y-1)(y-1)=0$$

 $y=\frac{1}{8}y=1$

$$y = \frac{1}{8} \quad y = 1$$
 $2^{2k} = \frac{1}{4} = \frac{1}{4} = 2^{-3} \quad \therefore \quad x = -3$

$$2^{2} = \frac{1}{8} = \frac{1}{2^{3}} = 2^{-3}$$
 : $x = -3$

(a) Factorise completely $9x - 4x^3$

 $y = 9x - 4x^3$

0,3,-3

Show on your sketch the coordinates at which the curve meets the *x*-axis.

(3)

(3)

(4)

The points A and B lie on C and have x coordinates of -2 and 1 respectively.

(c) Show that the length of AB is $k\sqrt{10}$ where k is a constant to be found.

$$x) x(9-4x^2) = x(3-2x)(3+2x)$$

c)
$$\chi = -2$$
 $y = 9(-2) - 4(-2)^3 = -18 + 32 = 14$

$$x=1$$
 $y=9(1)-4(1)^3=5$

(-2,14)
AB²=9²+3²=81+9=90
AB=
$$\sqrt{9}$$
0= $\sqrt{9}$ $\sqrt{10}$ =3 $\sqrt{10}$
3 (115)
 $\sqrt{8}$ $\sqrt{8}$ $\sqrt{8}$ $\sqrt{9}$ $\sqrt{9}$ $\sqrt{10}$ $\sqrt{9}$ $\sqrt{9}$

- Jess started work 20 years ago. In year 1 her annual salary was £17000. Her annual salary increased by £1500 each year, so that her annual salary in year 2 was £18500, in year 3 it was £20000 and so on, forming an arithmetic sequence. This continued until she reached her maximum annual salary of £32000 in year k. Her annual salary then remained at £32000.
 - (a) Find the value of the constant k.

(2)

(b) Calculate the total amount that Jess has earned in the 20 years.

(5)

$$S_{11} = \frac{1}{2} n(a+L) = \frac{11}{2} (17000 + 32000)$$

$$=\frac{11}{2} \times 49000$$
 $49 \times 11 = 539$ $(-2) = 269.5$

\$\$7500 £557500

$$S_{10} = \frac{1}{2}(10)(17000 + 30500) = 5 \times 47500$$

= 237500

557500

Given that
$$f'(x) = \frac{3\sqrt{x}}{2} - \frac{9}{4\sqrt{x}} + 2, \quad x > 0$$

(a) find
$$f(x)$$
, giving each term in its simplest form.

10. A curve with equation y = f(x) passes through the point (4, 9).

The normal to the curve at P is parallel to the line 2y + x = 0

The normal to the curve at
$$P$$
 is parallel to the line $2y + x = 0$
(b) Find the x coordinate of P .

Find the x coordinate of P.

$$3 = \frac{1}{2} - 9 = \frac{1}{2} + 2$$

a)
$$f'(x) = \frac{3}{2}x^{\frac{1}{2}} - \frac{9}{4}x^{-\frac{1}{2}} + 2$$

$$f(x) = \frac{3}{2}x^{\frac{2}{2}} - \frac{9}{4}x^{\frac{1}{2}} + 2x + C$$

$$f(z) = \chi^{\frac{3}{2}} - \frac{9}{2}\chi^{\frac{1}{2}} + 2\chi + C$$

$$(4,9) \Rightarrow 9 = (\sqrt{4})^3 - \frac{9}{2}\sqrt{4} + 8 + C \Rightarrow 9 = 8 - 9 + 8 + C$$

$$f(x) = \chi^{\frac{3}{2}} - \frac{9}{2}\chi^{\frac{1}{2}} + 2\chi + 2$$

$$f(x) = \chi^{\frac{3}{2}} - \frac{9}{2}\chi^{\frac{1}{2}} + 2\chi + 2$$

(5)

(5)

$$f(x) = \chi^{\frac{1}{2}} - \frac{9}{2}\chi^{\frac{1}{2}} + 2\chi + 2$$
b) $2y + \chi = 0 \Rightarrow y = -\frac{1}{2}\chi + 2\chi + 2$

$$h_{\lambda} = -\frac{1}{2} : M_{k} = 2 = f'(\chi)$$

$$\lambda = \frac{3}{2}\sqrt{2} - \frac{9}{4\sqrt{2}} + 2 = \frac{3}{2}\sqrt{2} - \frac{9}{4\sqrt{2}} = 0$$

$$= \frac{3}{2}\sqrt{x} = \frac{9}{4\sqrt{2}} = \frac{12x}{2} = 9 = \frac{100}{2} = \frac{100}$$